

CS240 Tutorial 6

1. Skip List Expected Height

Give a proof that the expected height of a skip list with n items is in $O(\log(n))$.

2. Modified AVL Height

Consider a modified version of an AVL tree called an AVL-2 Tree where we guarantee that for every node z in the tree that $|\text{height}(z.\text{left}) - \text{height}(z.\text{right})| \leq 2$. Prove that the height of an AVL-2 tree is in $O(\log(n))$

3. Always Rebalancing

Show that arbitrarily large AVL trees may require rotation at every node on the path to the root after deletion.